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# EchoTorch Documentation

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EchoTorch is an pyTorch-based library for Reservoir Computing and Echo State Network using GPUs and CPUs.



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## Echo State Network learning mechanics

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This note will present an overview of how Echo State Networks works works and its learning mechanics. It's not mandatory to understand the complete learning phase, but we recommend understanding the difference between classical ESN learning and gradient descent, it will help you to choose which one to use according to cases.

### 1.1 The Echo State Network model

#### 1.1.1 `esn_learning`





## 2.1 Subpackages

### 2.1.1 echotorch.datasets package

#### Submodules

##### echotorch.datasets.MackeyGlassDataset module

```
class echotorch.datasets.MackeyGlassDataset.MackeyGlassDataset (sample_len,  
                                                             n_samples,  
                                                             tau=17,  
                                                             seed=None)  
  
    Bases: torch.utils.data.dataset.Dataset  
    Mackey Glass dataset
```

##### echotorch.datasets.MemTestDataset module

```
class echotorch.datasets.MemTestDataset.MemTestDataset (sample_len,    n_samples,  
                                                         n_delays=10, seed=None)  
  
    Bases: torch.utils.data.dataset.Dataset  
  
    Generates a series of input timeseries and delayed versions as outputs. Delay is given in number of timesteps.  
    Can be used to empirically measure the memory capacity of a system.
```

##### echotorch.datasets.NARMADataSet module

```
class echotorch.datasets.NARMADataSet.NARMADataSet (sample_len,    n_samples,    sys-  
                                                         tem_order=10, seed=None)  
  
    Bases: torch.utils.data.dataset.Dataset
```

xth order NARMA task WARNING: this is an unstable dataset. There is a small chance the system becomes unstable, leading to an unusable dataset. It is better to use NARMA30 which where this problem happens less often.

## Module contents

**class** echotorch.datasets.**DatasetComposer** (*datasets, \*args, \*\*kwargs*)

Bases: torch.utils.data.dataset.Dataset

Compose dataset

**class** echotorch.datasets.**HenonAttractor** (*sample\_len, n\_samples, xy, a, b, washout=0, normalize=False, seed=None*)

Bases: torch.utils.data.dataset.Dataset

The Rössler attractor is the attractor for the Rössler system, a system of three non-linear ordinary differential equations originally studied by Otto Rössler. These differential equations define a continuous-time dynamical system that exhibits chaotic dynamics associated with the fractal properties of the attractor.

**regenerate** ()

Regenerate :return:

**class** echotorch.datasets.**LambdaDataset** (*sample\_len, n\_samples, func, start=0, dtype=torch.float32*)

Bases: torch.utils.data.dataset.Dataset

Create simple periodic signal timeseries

**class** echotorch.datasets.**LogisticMapDataset** (*sample\_len, n\_samples, alpha=5, beta=11, gamma=13, c=3.6, b=0.13, seed=None*)

Bases: torch.utils.data.dataset.Dataset

Logistic Map dataset

**class** echotorch.datasets.**LorenzAttractor** (*sample\_len, n\_samples, xyz, sigma, b, r, dt=0.01, washout=0, normalize=False, seed=None*)

Bases: torch.utils.data.dataset.Dataset

The Rössler attractor is the attractor for the Rössler system, a system of three non-linear ordinary differential equations originally studied by Otto Rössler. These differential equations define a continuous-time dynamical system that exhibits chaotic dynamics associated with the fractal properties of the attractor.

**regenerate** ()

Regenerate :return:

**class** echotorch.datasets.**MackeyGlassDataset** (*sample\_len, n\_samples, tau=17, seed=None*)

Bases: torch.utils.data.dataset.Dataset

Mackey Glass dataset

**class** echotorch.datasets.**MemTestDataset** (*sample\_len, n\_samples, n\_delays=10, seed=None*)

Bases: torch.utils.data.dataset.Dataset

Generates a series of input timeseries and delayed versions as outputs. Delay is given in number of timesteps. Can be used to empirically measure the memory capacity of a system.

**class** echotorch.datasets.**NARMADataset** (*sample\_len, n\_samples, system\_order=10, seed=None*)

Bases: torch.utils.data.dataset.Dataset

xth order NARMA task WARNING: this is an unstable dataset. There is a small chance the system becomes unstable, leading to an unusable dataset. It is better to use NARMA30 which where this problem happens less often.

```
class echotorch.datasets.RösslerAttractor (sample_len, n_samples, xyz, a, b, c, dt=0.01,  
                                         washout=0, normalize=False, seed=None)
```

Bases: torch.utils.data.dataset.Dataset

The Rössler attractor is the attractor for the Rössler system, a system of three non-linear ordinary differential equations originally studied by Otto Rössler. These differential equations define a continuous-time dynamical system that exhibits chaotic dynamics associated with the fractal properties of the attractor.

**regenerate** ()

Regenerate :return:

```
class echotorch.datasets.SinusoidalTimeseries (sample_len, n_samples, period, a=1.0,  
                                              m=0.0, start=1, dtype=torch.float64)
```

Bases: torch.utils.data.dataset.Dataset

Sinusoidal timeseries

**random\_initial\_points** ()

Random initial points :return:

**regenerate** ()

Regenerate :return:

```
class echotorch.datasets.PeriodicSignalDataset (sample_len, n_samples, period, start=1,  
                                              dtype=torch.float64)
```

Bases: torch.utils.data.dataset.Dataset

Create simple periodic signal timeseries

## 2.1.2 echotorch.nn

### Echo State Layers

#### ESNCell

```
class nn.ESNCell (input_dim, output_dim, spectral_radius=0.9, bias_scaling=0, input_scaling=1.0,  
                  w=None, w_in=None, w_bias=None, w_fdb=None, sparsity=None, input_set=[1.0,  
                  -1.0], w_sparsity=None, nonlin_func=<built-in function tanh>, feedbacks=False,  
                  feedbacks_dim=None, wfdb_sparsity=None, normalize_feedbacks=False,  
                  seed=None, w_distrib='uniform', win_distrib='uniform', wbias_distrib='uniform',  
                  win_normal=(0.0, 1.0), w_normal=(0.0, 1.0), wbias_normal=(0.0, 1.0),  
                  dtype=torch.float32)
```

Echo State Network layer

**forward** (*u, y=None, w\_out=None, reset\_state=True*)

Forward :param u: Input signal :param y: Target output signal for teacher forcing :param w\_out: Output weights for teacher forcing :return: Resulting hidden states

**static generate\_gaussian\_matrix** (*size, sparsity, mean=0.0, std=1.0, dtype=torch.float32*)

Generate gaussian Win matrix :return:

**static generate\_uniform\_matrix** (*size, sparsity, input\_set*)

Generate uniform Win matrix :param w\_in: :param seed: :return:

```
static generate_w(output_dim, w_distrib='uniform', w_sparsity=None, mean=0.0, std=1.0,
                  seed=None, dtype=torch.float32)
    Generate W matrix :param output_dim: :param w_sparsity: :return:

get_spectral_radius()
    Get W's spectral radius :return: W's spectral radius

init_hidden()
    Init hidden layer :return: Initiated hidden layer

reset_hidden()
    Reset hidden layer :return:

set_hidden(x)
    Set hidden layer :param x: :return:

static to_sparse(m)
    To sparse matrix :param m: :return:
```

## ESN

```
class nn.ESN(input_dim, hidden_dim, output_dim, spectral_radius=0.9, bias_scaling=0,
              input_scaling=1.0, w=None, w_in=None, w_bias=None, w_fdb=None, sparsity=None,
              input_set=[1.0, -1.0], w_sparsity=None, nonlin_func=<built-in function tanh>, learning_algo='inv',
              ridge_param=0.0, create_cell=True, feedbacks=False, with_bias=True, wfdb_sparsity=None,
              normalize_feedbacks=False, softmax_output=False, seed=None, washout=0, w_distrib='uniform',
              win_distrib='uniform', wbias_distrib='uniform', win_normal=(0.0, 1.0), w_normal=(0.0, 1.0),
              wbias_normal=(0.0, 1.0), dtype=torch.float32)
```

Echo State Network module

```
finalize()
    Finalize training with LU factorization

forward(u, y=None, reset_state=True)
    Forward :param u: Input signal. :param y: Target outputs :return: Output or hidden states

get_spectral_radius()
    Get W's spectral radius :return: W's spectral radius

get_w_out()
    Output matrix :return:

hidden
    Hidden layer :return:

reset()
    Reset learning :return:

reset_hidden()
    Reset hidden layer :return:

set_w(w)
    Set W :param w: :return:

w
    Hidden weight matrix :return:

w_in
    Input matrix :return:
```

## LiESNCell

```
class nn.LiESNCell (leaky_rate=1.0, train_leaky_rate=False, *args, **kwargs)
    Leaky-Integrated Echo State Network layer

    forward (u, y=None, w_out=None, reset_state=True)
        Forward :param u: Input signal. :return: Resulting hidden states.
```

## LiESN

```
class nn.LiESN (input_dim, hidden_dim, output_dim, spectral_radius=0.9, bias_scaling=0, input_scaling=1.0, w=None, w_in=None, w_bias=None, sparsity=None, input_set=[1.0, -1.0], w_sparsity=None, nonlin_func=<built-in function tanh>, learning_algo='inv', ridge_param=0.0, leaky_rate=1.0, train_leaky_rate=False, feedbacks=False, wfdb_sparsity=None, normalize_feedbacks=False, softmax_output=False, seed=None, washout=0, w_distrib='uniform', win_distrib='uniform', wbias_distrib='uniform', win_normal=(0.0, 1.0), w_normal=(0.0, 1.0), wbias_normal=(0.0, 1.0), dtype=torch.float32)
    Leaky-Integrated Echo State Network module
```

## 2.1.3 echotorch.tools package

### Submodules

#### echotorch.utils.error\_measures module

```
echotorch.utils.error_measures.cumperplexity (output_probs, targets, log=False)
    Cumulative perplexity :param output_probs: :param targets: :param log: :return:

echotorch.utils.error_measures.generalized_squared_cosine (Sa, Ua, Sb, Ub)
    Generalized square cosine :param Sa: :param Ua: :param Sb: :param Ub: :return:

echotorch.utils.error_measures.mse (outputs, targets)
    Mean square error :param outputs: Module's outputs :param targets: Target signal to be learned :return: Mean square deviation

echotorch.utils.error_measures.nmse (outputs, targets)
    Normalized mean square error :param outputs: Module's output :param targets: Target signal to be learned :return: Normalized mean square deviation

echotorch.utils.error_measures.normse (outputs, targets)
    Normalized root-mean square error :param outputs: Module's outputs :param targets: Target signal to be learned :return: Normalized root-mean square deviation

echotorch.utils.error_measures.perplexity (output_probs, targets, log=False)
    Perplexity :param output_probs: Output probabilities for each word/tokens (length x n_tokens) :param targets: Real word index :return: Perplexity

echotorch.utils.error_measures.rmse (outputs, targets)
    Root-mean square error :param outputs: Module's outputs :param targets: Target signal to be learned :return: Root-mean square deviation
```

## echotorch.utils.utility\_functions module

`echotorch.utils.utility_functions.align_pattern` (*interpolation\_rate*, *truth\_pattern*, *generated\_pattern*)  
Align pattern :param interpolation\_rate: :param truth\_pattern: :param generated\_pattern: :return:

`echotorch.utils.utility_functions.average_prob` (*tensor*, *dim=0*)  
Average probabilities through time :param tensor: :param dim: :return:

`echotorch.utils.utility_functions.compute_correlation_matrix` (*states*)  
Compute correlation matrix :param states: :return:

`echotorch.utils.utility_functions.compute_similarity_matrix` (*svd\_list*)  
Compute similarity matrix :param svd\_list: :return:

`echotorch.utils.utility_functions.compute_singular_values` (*stats*)  
Compute singular values :param states: :return:

`echotorch.utils.utility_functions.deep_spectral_radius` (*m*, *leaky\_rate*)  
Compute spectral radius of a square 2-D tensor for stacked-ESN :param m: squared 2D tensor :param leaky\_rate: Layer's leaky rate :return:

`echotorch.utils.utility_functions.find_phase_shift` (*p*, *y*, *interpolation\_rate*, *error\_measure=<function nrmse>*)  
Find phase shift :param s1: :param s2: :param window\_size: :return:

`echotorch.utils.utility_functions.max_average_through_time` (*tensor*, *dim=0*)  
Max average through time :param tensor: :param dim: Time dimension :return:

`echotorch.utils.utility_functions.normalize` (*tensor*, *dim=1*)  
Normalize a tensor on a single dimension :param t: :return:

`echotorch.utils.utility_functions.spectral_radius` (*m*)  
Compute spectral radius of a square 2-D tensor :param m: squared 2D tensor :return:

## Module contents

`echotorch.utils.align_pattern` (*interpolation\_rate*, *truth\_pattern*, *generated\_pattern*)  
Align pattern :param interpolation\_rate: :param truth\_pattern: :param generated\_pattern: :return:

`echotorch.utils.compute_correlation_matrix` (*states*)  
Compute correlation matrix :param states: :return:

`echotorch.utils.nrmse` (*outputs*, *targets*)  
Normalized root-mean square error :param outputs: Module's outputs :param targets: Target signal to be learned :return: Normalized root-mean square deviation

`echotorch.utils.nmse` (*outputs*, *targets*)  
Normalized mean square error :param outputs: Module's output :param targets: Target signal to be learned :return: Normalized mean square deviation

`echotorch.utils.rmse` (*outputs*, *targets*)  
Root-mean square error :param outputs: Module's outputs :param targets: Target signal to be learned :return: Root-mean square deviation

`echotorch.utils.mse` (*outputs*, *targets*)  
Mean square error :param outputs: Module's outputs :param targets: Target signal to be learned :return: Mean square deviation

---

```

echotorch.utils.perplexity (output_probs, targets, log=False)
    Perplexity :param output_probs: Output probabilities for each word/tokens (length x n_tokens) :param targets:
    Real word index :return: Perplexity

echotorch.utils.cumperplexity (output_probs, targets, log=False)
    Cumulative perplexity :param output_probs: :param targets: :param log: :return:

echotorch.utils.spectral_radius (m)
    Compute spectral radius of a square 2-D tensor :param m: squared 2D tensor :return:

echotorch.utils.deep_spectral_radius (m, leaky_rate)
    Compute spectral radius of a square 2-D tensor for stacked-ESN :param m: squared 2D tensor :param leaky_rate:
    Layer's leaky rate :return:

echotorch.utils.normalize (tensor, dim=1)
    Normalize a tensor on a single dimension :param t: :return:

echotorch.utils.average_prob (tensor, dim=0)
    Average probabilities through time :param tensor: :param dim: :return:

echotorch.utils.max_average_through_time (tensor, dim=0)
    Max average through time :param tensor: :param dim: Time dimension :return:

echotorch.utils.show_3d_timeseries (ts, title)
    Show 3D timeseries :param axis: :param title: :return:

echotorch.utils.show_2d_timeseries (ts, title)
    Show 2D timeseries :param ts: :param title: :return:

echotorch.utils.show_1d_timeseries (ts, title, xmin, xmax, ymin, ymax, start=0, timesteps=-1)
    Show 1D time series :param ts: :param title: :return:

echotorch.utils.neurons_activities_1d (stats, neurons, title, colors, xmin, xmax, ymin, ymax,
                                     timesteps=-1, start=0)
    Display neurons activities :param stats: :param neurons: :return:

echotorch.utils.neurons_activities_2d (stats, neurons, title, colors, timesteps=-1, start=0)
    Display neurons activities on a 2D plot :param stats: :param neurons: :param title: :param timesteps: :param
    start: :return:

echotorch.utils.neurons_activities_3d (stats, neurons, title, timesteps=-1, start=0)
    Display neurons activities on a 3D plot :param stats: :param neurons: :param title: :param timesteps: :param
    start: :return:

echotorch.utils.plot_singular_values (stats, title, xmin, xmax, ymin, ymax, log=False)
    Plot singular values :param stats: :param title: :param timestep: :param start: :return:

echotorch.utils.compute_singular_values (stats)
    Compute singular values :param states: :return:

echotorch.utils.generalized_squared_cosine (Sa, Ua, Sb, Ub)
    Generalized square cosine :param Sa: :param Ua: :param Sb: :param Ub: :return:

echotorch.utils.compute_similarity_matrix (svd_list)
    Compute similarity matrix :param svd_list: :return:

echotorch.utils.show_similarity_matrix (sim_matrix, title, column_labels=None,
                                     row_labels=None)
    Show similarity matrix :param sim_matrix: :return:

echotorch.utils.show_conceptors_similarity_matrix (conceptors, title)
    Show conceptors similarity matrix :param conceptors: :param title: :return:

```

`echotorch.utils.show_sv_for_increasing_aperture` (*conceptor*, *factor*, *title*)

Show singular values for increasing aperture :param conceptors: :param factor: :param title: :return:

`echotorch.utils.find_phase_shift` (*p*, *y*, *interpolation\_rate*, *error\_measure*=<function nrmse>)

Find phase shift :param s1: :param s2: :param window\_size: :return:

## 2.2 Module contents



## CHAPTER 3

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